

CSE467: Computer Security

3. Classical Cryptography

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Recap: <u>CIA</u> Properties

- Confidentiality: information is not made available to unauthorized parties
- Integrity: information is not modified in an unauthorized manner
- Availability: information is readily available when it is needed
- + Authentication, Non-repudiation



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Basic Terminology

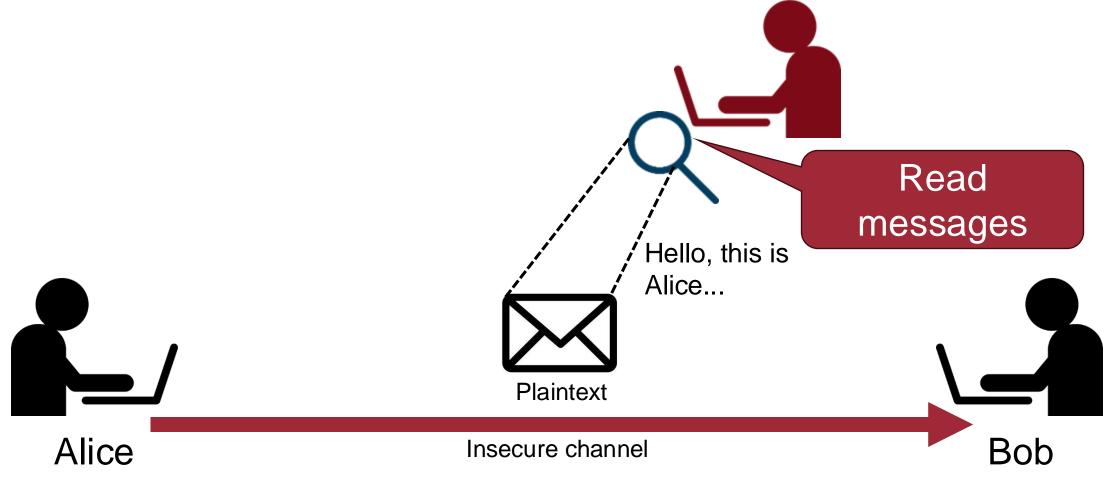
- Plaintext: original message
- Ciphertext: coded message
- Key: info used in cipher known only to sender/receiver
- Cipher: algorithm for transforming some texts
 - -Encipher (encrypt): converting plaintext to ciphertext
 - -Decipher (decrypt): recovering ciphertext from plaintext





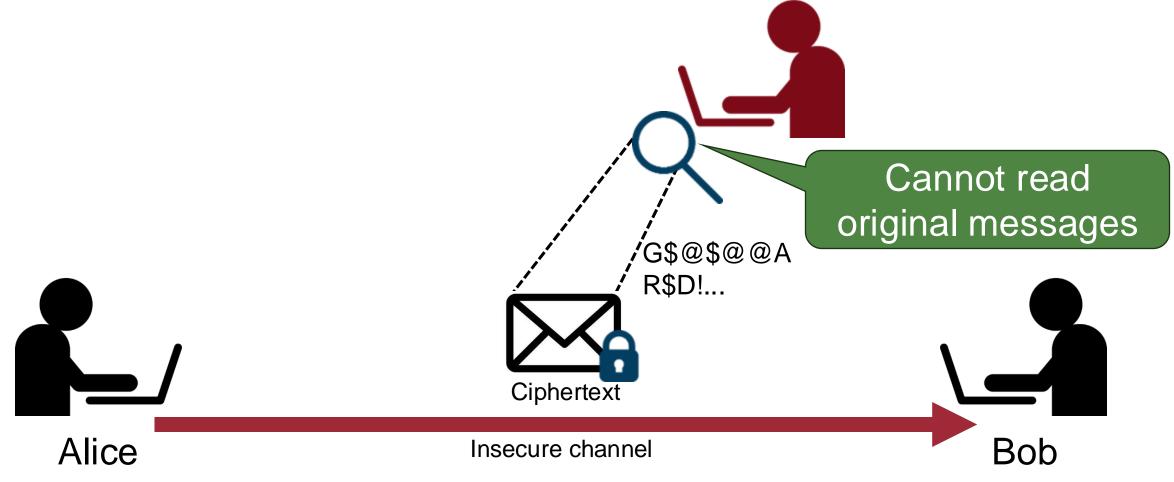
Cryptography

- "Secret writing" in Greek
- Goal: protect your (sensitive) messages/data from eavesdropping



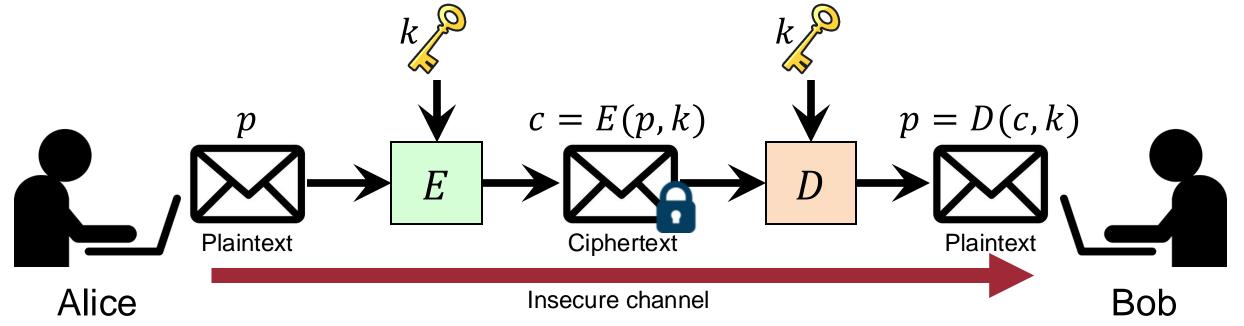
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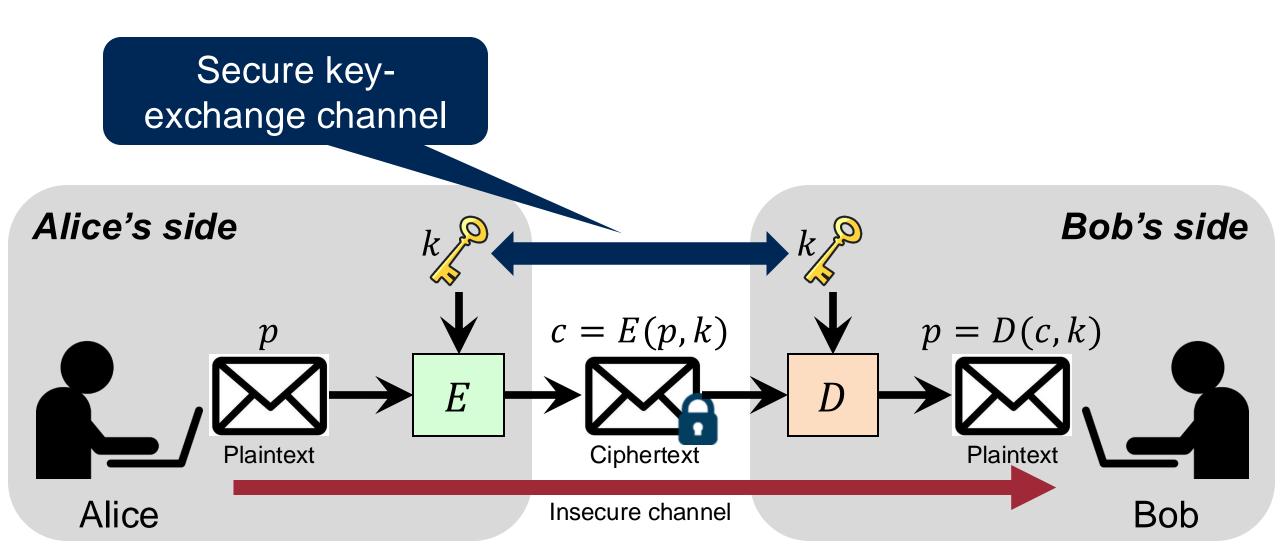


Cryptography

- "Secret writing" in Greek
- Goal: protect your (sensitive) messages/data from eavesdropping
- The most basic building block of computer security
- Two functions: encryption (E) and decryption (D) parameterized by a plaintext (p), ciphertext (c), and cryptographic key (k)



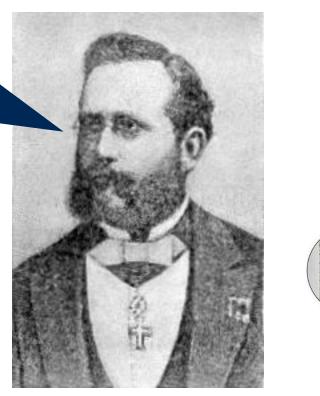
(Symmetric Key) Cryptography



Kerckhoff's Principle



- Auguste Kerckhoffs

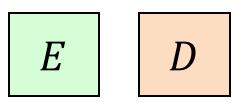


Secret! Publicly known

The resistance of the cipher must be based only on the secrecy of the key

Requirements in Symmetric Encryption

- 1. A strong encryption algorithm
 - -Assume encryption algorithm is known



- 2. The secrecy of the key
 - -A secret key known only to sender / receiver
 - -Must be unpredictable 🔊

Classical vs. Modern

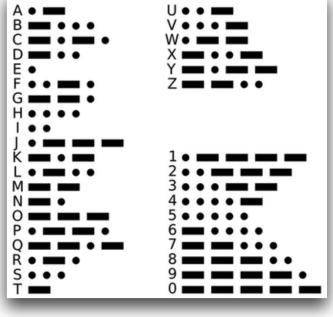
• Cryptography: "The art of writing or solving codes" (Oxford English Dictionary)

Codes

- -For secret communications: confidentiality
- -*Modern cryptography* includes more: integrity, non-repudiation, secret key exchange, etc.

• Art

- -Little theory but ad-hoc designs
- -Modern cryptography: science and math



Classical Cryptography

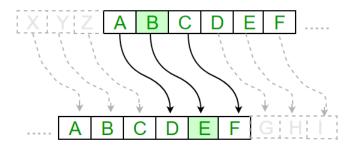
Classical Cryptography

- CAUTION: DO NOT use this classical cryptography for any practical uses
- Why do we study classical ones?
 - To highlight the weakness of ad-hoc approaches
 - To demonstrate that simple approaches are unlikely to succeed
- In this lecture, we will cover
 - Caesar cipher
 - Substitution cipher
 - Vigenere cipher

Classical Cryptography – Caesar Cipher

- Encryption: shift each plaintext character 3 places forward
- Example:
 - -Plaintext: insukseo
 - -Ciphertext: lqvxnvhr
- Q. What is the key?





Classical Cryptography – Caesar Cipher

• Encryption: shift each plaintext character k places forward

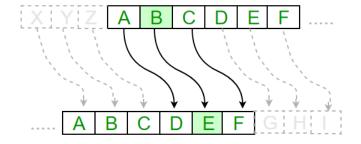
$$E(p,k) = (p+k) \mod 26$$

$$D(c,k) = (c-k) \mod 26$$

Q. How many other keys could be chosen?

Q. Robust enough?





Problem: Exhaustive Key Search

- Key: a number between 0 and 25
- Given a cipher text: ovdthufwvzzpislrlfzhylaolyl
- Can you find the plaintext? How?

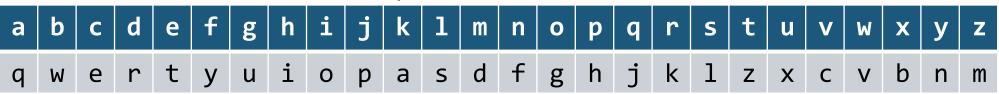
Key Value	Possible Plain Text
1	nucsgtevuyyohrkqkeygxkznkxk
2	mtbrfsdutxxngqjpjdxfwjymjwj
3	lsaqerctswwmfpioicwevixlivi
7	howmanypossiblekeysarethere

How to make it more robust?



Classical Cryptography – Substitution Cipler

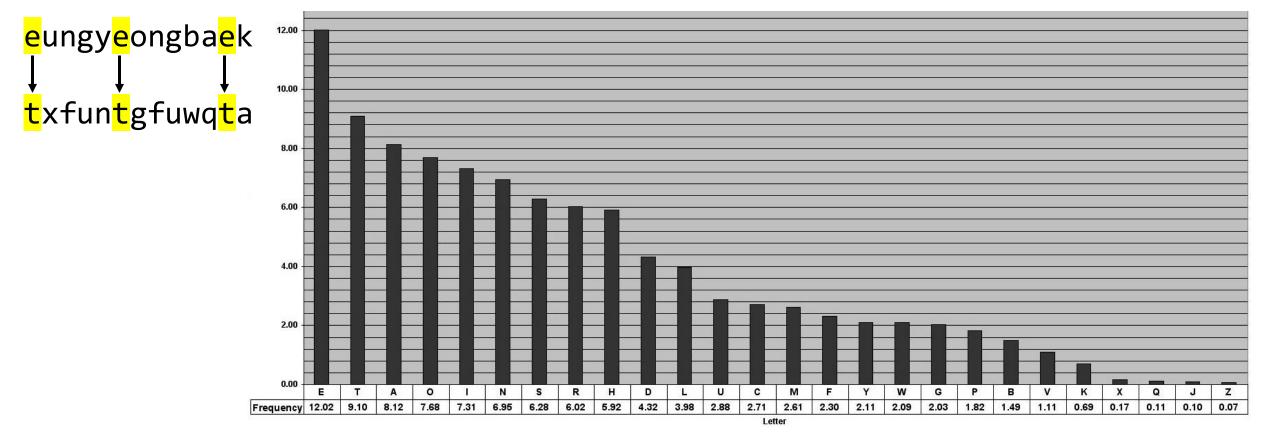
- One-to-one mapping (bijection)
- Example:
 - Plaintext: eungyeongbaek
 - -Key: Substitution mapping table



- Ciphertext: txfuntgfuwqta
- Key space?
- Q. Robust enough?

Problem: Letter Frequency Analysis

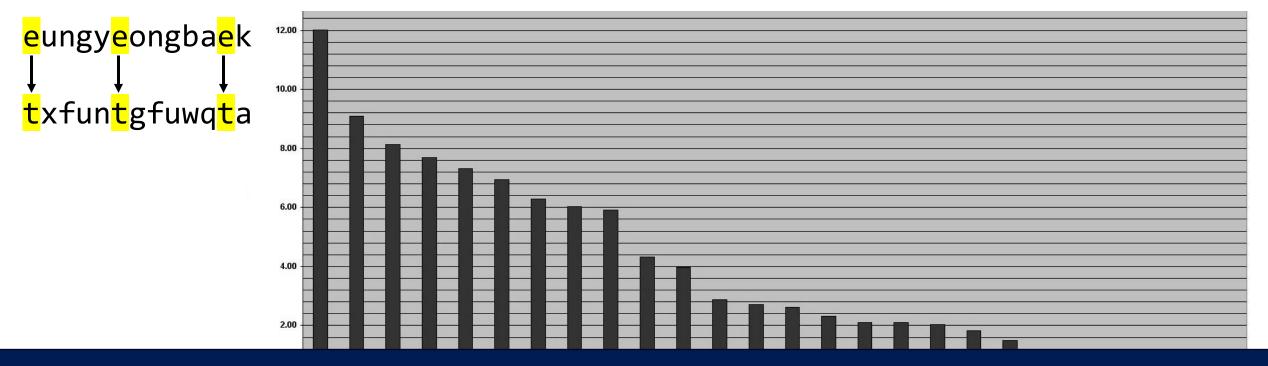
 Observation: Each plaintext symbol always maps to the same ciphertext symbol



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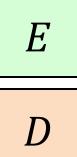
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How to make it more robust?

Classical Cryptography – Vigenere Cipher

• Encryption: poly-alphabetic shift



$$E(p,k) = (p_i + k_i) \mod 26$$

 $D(c,k) = (c_i - k_i) \mod 26$

Invented in 16th century and had been unbreakable for hundreds of years!



- Example
 - Plaintext:
 - -Key (repeated):
 - Ciphertext:

tellhimaboutme
cafecafecafeca
veqpjiredozxoe

• Letters are mapped to different ciphertexts: smooth out the frequency distribution in ciphertext

Cracking Vigenere Cipher

- When the length t (e.g., 4) of the key is known:
 - Divide ciphertext into t parts and perform statistical analysis for each part

Plaintext:tellhimaboutmeKey (repeated):cafecafecafecaEach plaintext symbolCiphertext:veqpjiredozxoealways maps to the
same ciphertext symbol

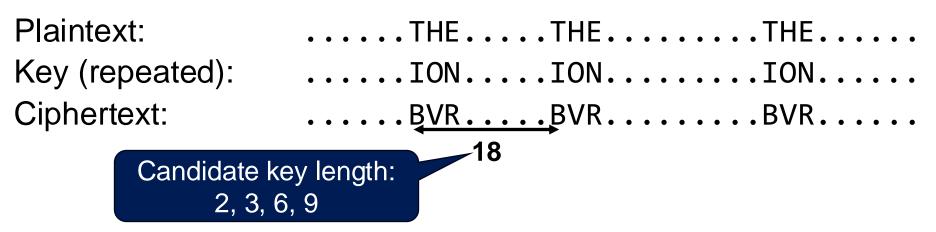
- -When the length t is unknown but the max length T is known:
 - Repeat the above *T* times (*t* = 1, 2, 3, ..., *T*)
- What if the length is unknown?

Kasiski's Method



- Goal: extract the length t of the key
- Observations:
 - A repeated substring may exist in the ciphertext
 - The distance of the two occurrences may be a multiple of the key length

• Example:

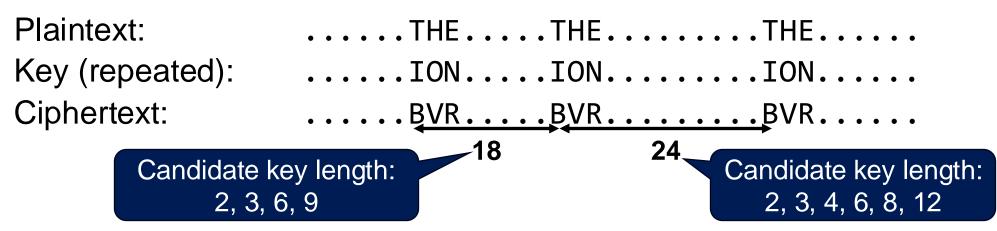


Friedrich W. Kasiski, Die Geheimschriften und die Dechiffrirkunst, Mittler und Sohn, Berlin, 1863

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LFWKI MJCLP SISWK HJOGL KMVGU RAGKM KMXMA MJCVX WUYLG GIISW ALXAE YCXMF KMKBQ BDCLA EFLFW KIMJC GUZUG SKECZ GBWYM OACFV MQKYF WXTWM LAIDO YQBWF GKSDI ULQGV SYHJA VEFWB LAEFL FWKIM JCFHS NNGGN WPWDA VMQFA AXWFZ CXBVE LKWML AVGKY EDEMJ XHUXD AVYXL





Idx 0 LFWKI MJCLP SISWK HJOGL KMVGU RAGKM KAXMA MJCVX WUYLG GIISW ALXAE YCXMF KMKBQ BDCLA EFLFW KIMJC GUZUG SKECZ GBWYM OACFV MQKYF WXTWM LAIDO YQBWF GKSDI ULQGV SYHJA VEFWB LAEFL FWKIM JCFHS NNGGN WPWDA VMQFA AXWFZ CXBVE LKWIL AVGKY EDEMJ XHUXD AVYXL Idx 144

- Substring: LFWKIMJC
- Position: Idx 0, 72, 144
- Distance: 72





LFWKI MJCLP SISWK HJOGL KMVGU RAGKM KMXMA MJCVX WUYLG GIISW ALXAE YCXMF KMKBQ BDCLA EFLFW KIMJC GUZUG SKECZ GBWYM OACFV MQKYF WXTWM LAIDO YQBWF GKSDI ULQGV SYHJA VEFWB LAEFL FWKIM JCFHS NNGGN WPWDA VMQFA AXWFZ CXBVE LKWML AVGKY EDEMJ XHUXD AVYXL

- Substring: WMLA
- Position: Idx 108, 182
- Distance: 74





LFWKI MJCLP SISWK HJOGL KMVGU RAGKM KMXMA MJCVX WUYLG GIISW ALXAE YCXMF KMKBQ BDCLA EFLFW KIMJC GUZUG SKECZ GBWYM OACFV MQKYF WXTWM LAIDO YQBWF GKSDI ULQGV SYHJA VEFWB LAEFL FWKIM JCFHS NNGGN WPWDA VMQFA AXWFZ CXBVE LKWML AVGKY EDEMJ XHUXD AVYXL

- Substring: ISW
- Position: Idx 11, 47
- Distance: 36





Substring	Distance	Factors (divisors, 약수)
LFWKIMJC	72	2 3 4 6 8 9 12 18 24 36 72
WMLA	74	2 37 74
MJC	66	2 3 6 11 22 33 66
ISW	36	23469121836
VMQ	32	2 4 8 16 32
DAV	30	23561015

¥



		Factors																	
	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
74	0																		
72	0	0	0		0		0	0			0						0		
66	0	0			0					0									
36	0	0	0		0			0			0						0		
32	0		0				0								0				
30	0	0		0	0				0					0					
Total	6	4	3	1	4	0	2	2	1	1	2	0	0	1	1	0	2	0	0

₩

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Top candidates

Result



LFWKI MJCLP SISWK HJOGL KMVGU RAGKM KMXMA MJCVX WUYLG GIISW ALXAE YCXMF KMKBQ BDCLA EFLFW KIMJC GUZUG SKECZ GBWYM OACFV MQKYF WXTWM LAIDO YQBWF GKSDI ULQGV SYHJA VEFWB LAEFL FWKIM JCFHS NNGGN WPWDA VMQFA AXWFZ CXBVE LKWML AVGKY EDEMJ XHUXD AVYXL

THERE ARETW OWAYS OFCON STRUC TINGA SOFTW AREDE SIGNO NEWAY ISTOM AKEIT SOSIM PLETH ATTHE REARE OBVIO USLYN ODEFI CIENC IESAN DTHEO THERW AYIST OMAKE ITSOC OMPLI CATED THATT HEREA RENOO BVIOU SDEFI CIENC IESTH EFIRS TMETH ODISF ARMOR EDIFF ICULT

Pop-up Lesson



"There are two ways of constructing a software design: One way is to make it so simple that there are obviously no deficiencies, and the other way is to make it so complicated that there are no obvious deficiencies. The first method is far more difficult."

- T. Hoare, ACM Turing Award winner (1980)



Properties of Kasiski's Method

Object	Property
Long ciphertext	
Short plaintext	
Long repeated substrings in a ciphertext	
Short repeated substrings in a ciphertext	

Introduction to Modern Cryptography

Principles of Modern Cryptography

- Rigorous approaches to security
- What we need for science?
 - Formal (i.e., rigorous and precise) definitions of security
 - Precise assumptions
 - Proofs of security

Formal Definition

- Can you formally define what you mean by "security"?
- Security definition is a tuple
 - Adversary assumptions (threat modeling): "power (or capabilities) of the adversary"
 - Security guarantee: "what the scheme is intended to prevent the assumed attack"

- Example
 - Assume: magnitude ≤ 7 earthquake
 - Guarantee: nuclear power plant does not collapse

Security Guarantees

- Example: What are the **desired security guarantees** for secure encryption?
- Impossible for an attacker
 - To recover the key! Enough?
 - To recover the entire plaintext from the ciphertext! Enough?
 - To recover any character of the plaintext from the ciphertext! Enough?
 - To derive any meaningful information about the plaintext from the ciphertext! Enough?

Cryptanalysis



- Study of principles/methods of decrypting ciphertext without using the real key
- Objective: to recover the key messages without actually knowing the key
- General approaches
 - Cryptanalytic attack
 - Brute-force attack

Cryptanalytic attack - Adversary Assumptions ³⁸

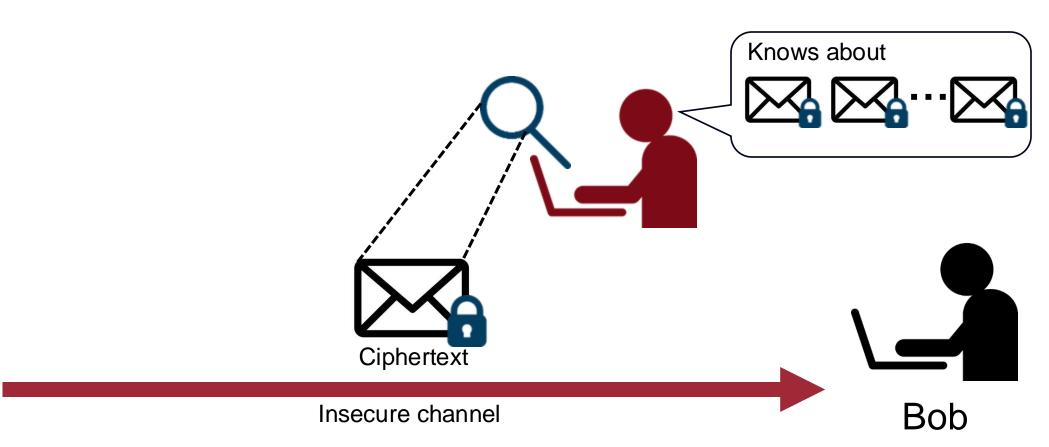
- What are the <u>adversary capabilities</u>?
- Attacker capabilities (in order of increasing attack power)
 - Ciphertext-only attack: most basic attack
 - Known-plaintext attack: attacker obtains certain plaintext/ciphertext pairs
 - Chosen-plaintext attack: attacker obtains plaintext/ciphertext pairs for plaintext of its choice
 - Chosen-ciphertext attack: attacker obtains plaintext/ciphertext pairs for ciphertext of its choice

Ciphertext-Only Attack (COA)

• Most basic attack

Alice

• The attacker is assumed to have access only to ciphertexts



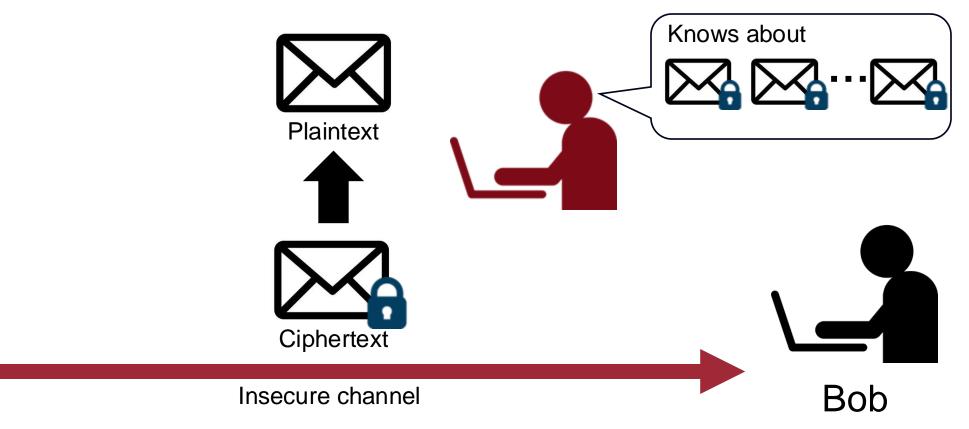
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Ciphertext-Only Attack (COA)

• Most basic attack

Alice

- The attacker is assumed to have access only to ciphertexts
- Can the attacker compute the key from the ciphertext?

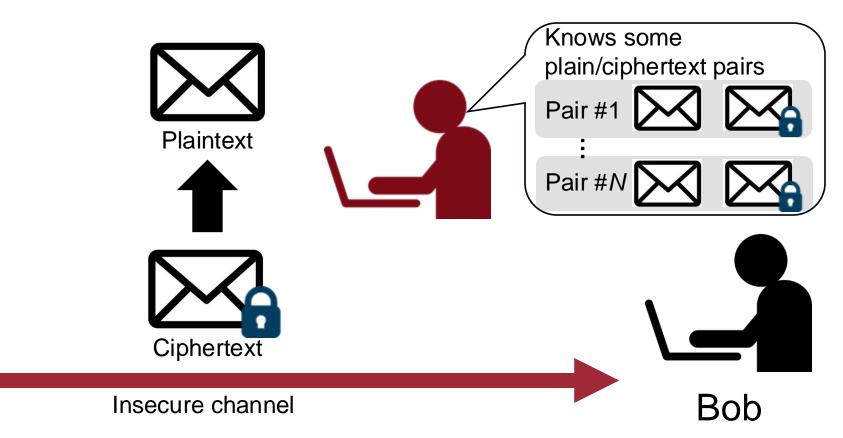


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Known-Plaintext Attack (KPA)

Alice

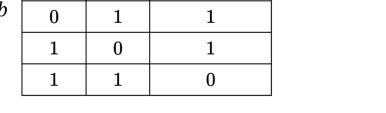
- The attacker is assumed to have access to multiple plaintexts and their corresponding ciphertexts
- Can the attacker compute the key from the ciphertext?

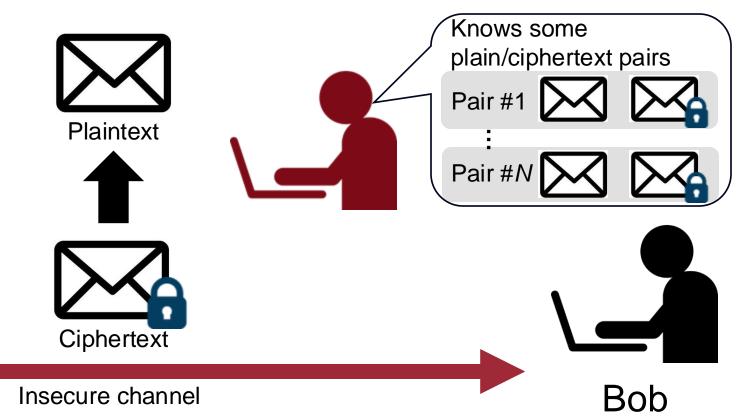


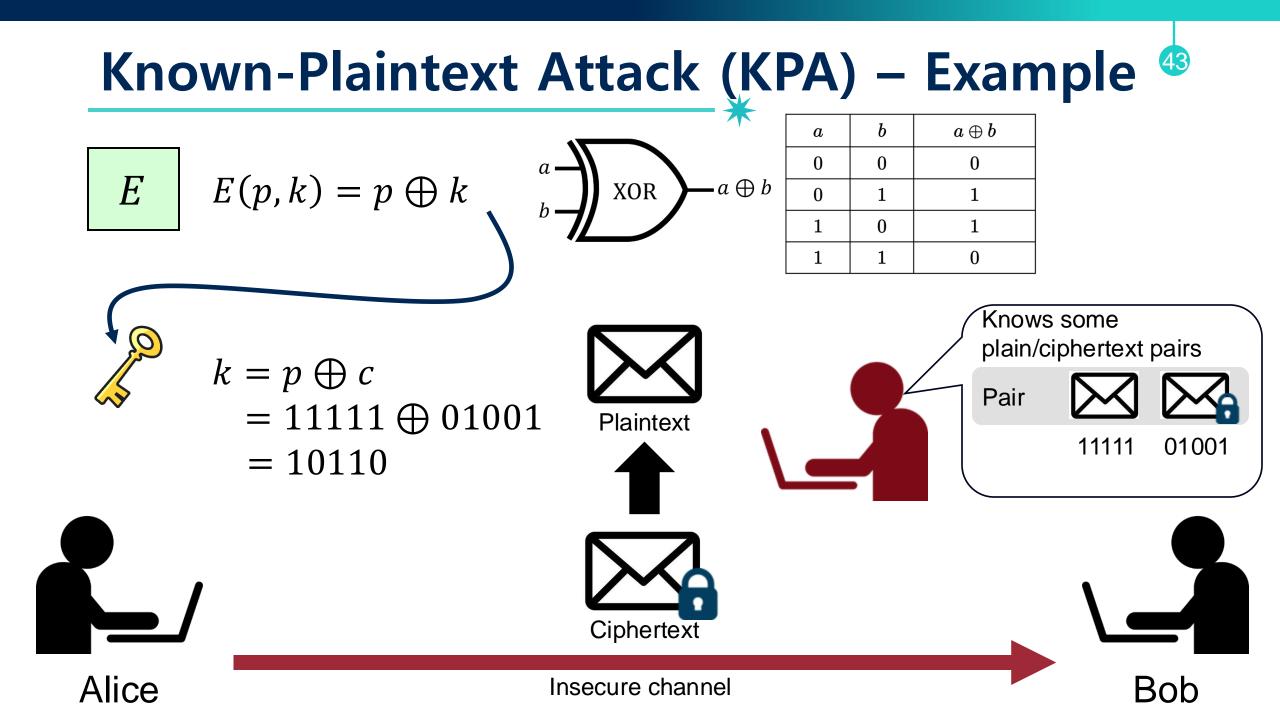
Known-Plaintext Attack (KPA) – Example 🍄

$$E \qquad E(p,k) = p \oplus k$$

Alice

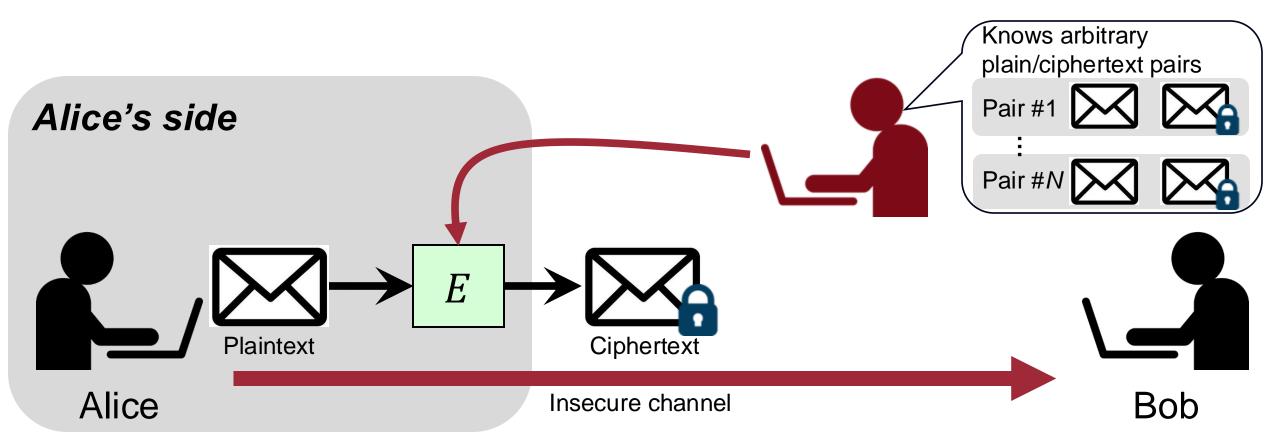




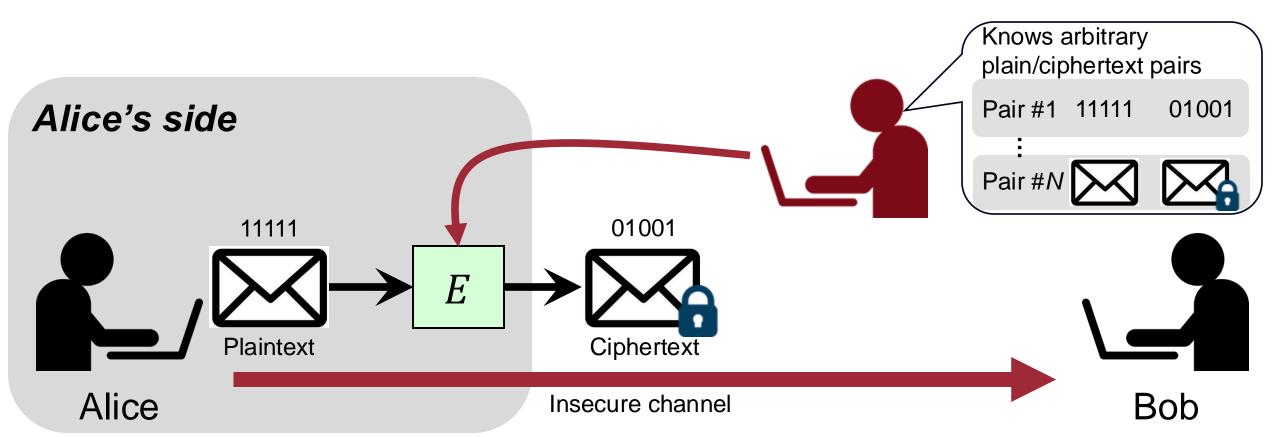


Chosen-Plaintext Attack (CPA)

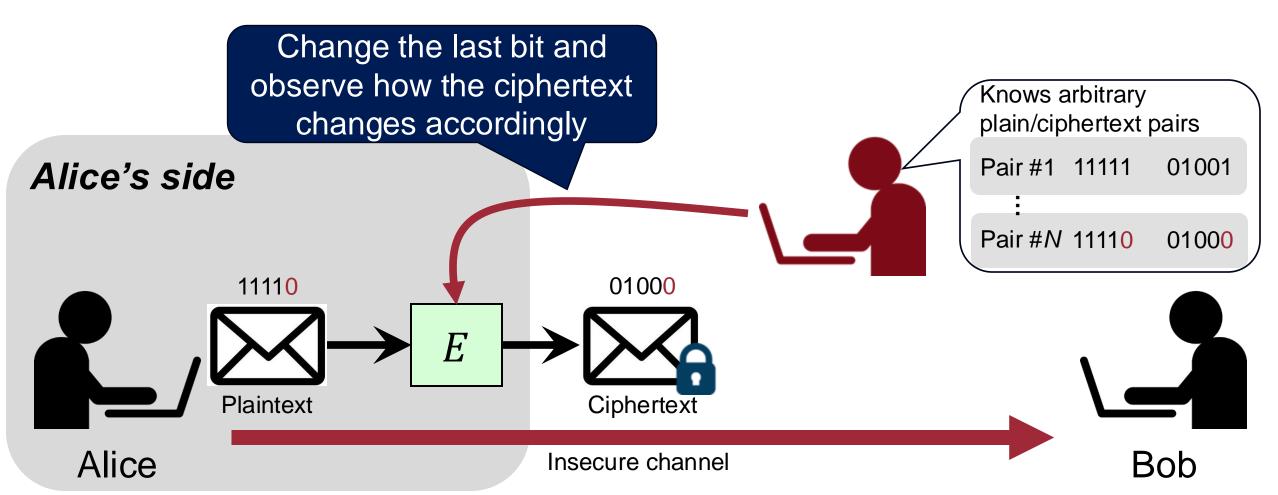
• The attacker is able to <u>define his own plaintext</u>, feed it into the encryption algorithm, and <u>analyze the resulting ciphertext</u>



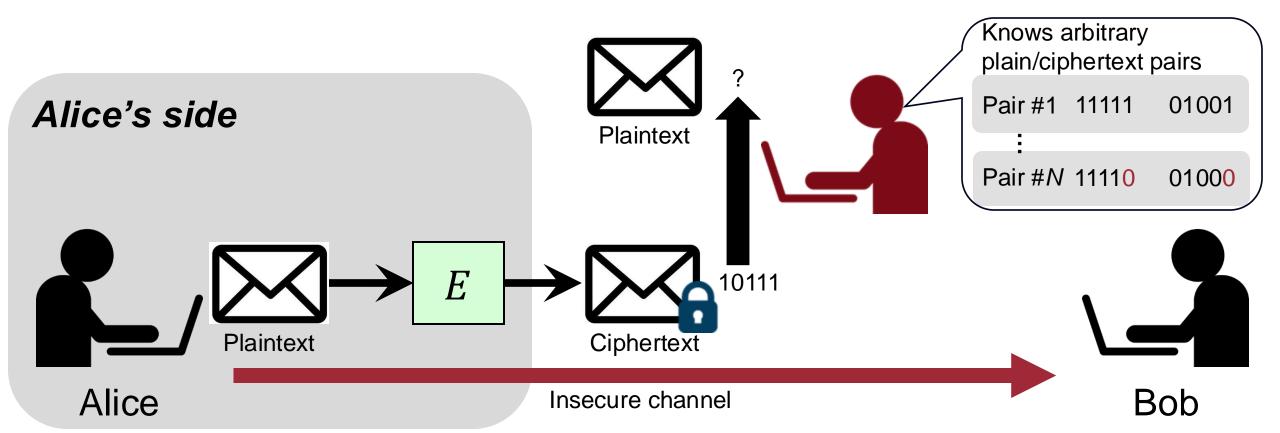
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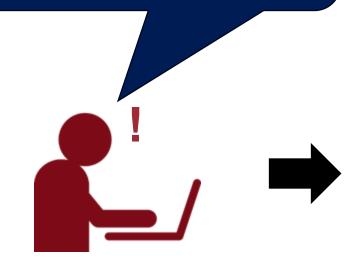


- The bit we vary is consistently negated
- ✓ As one bit varies, the remaining ones are left unchanged



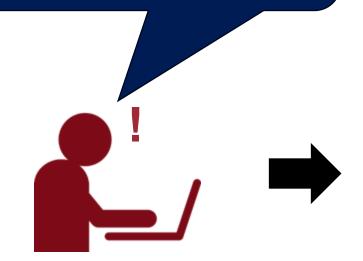
	Plaintext	Ciphertext
Try #1	11111	01001
Try #2	1111 <mark>0</mark>	01000
Try #3	111 <mark>0</mark> 1	01011
Try #4	11 <mark>0</mark> 11	01101
Try #5	1 <mark>0</mark> 111	00001
Try #6	<mark>0</mark> 1111	1 1001

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		10111

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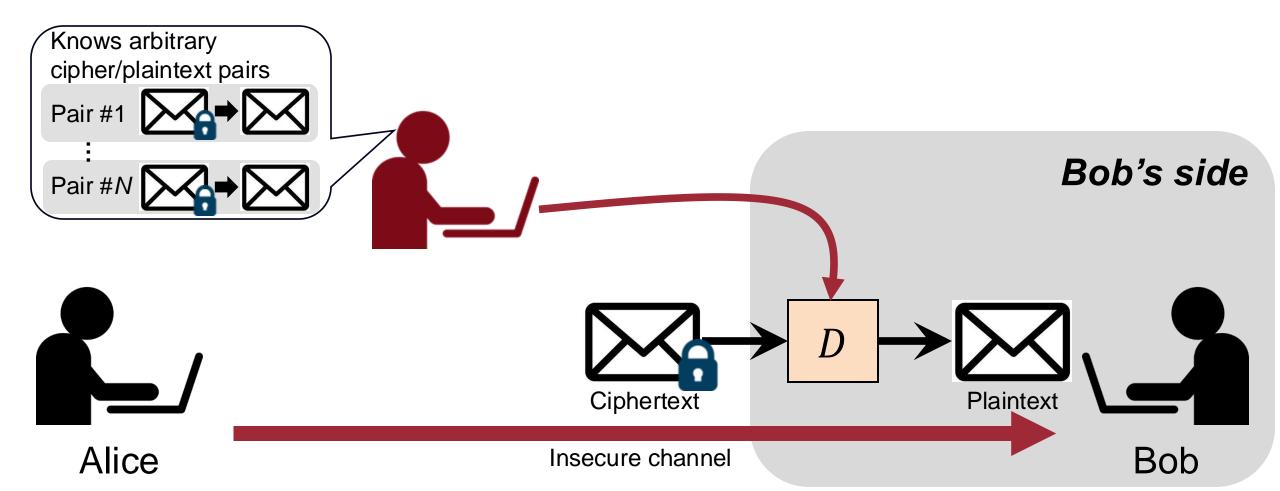


	Plaintext	Ciphertext
Try #1	11111	01001
Try #2	1111 <mark>0</mark>	01000
Try #3	111 <mark>0</mark> 1	010 <mark>1</mark> 1
Try #4	11 <mark>0</mark> 11	01101
Try #5	1 <mark>0</mark> 111	00001
Try #6	<mark>0</mark> 1111	11001
Final	00001 🔶	10111

Chosen-Ciphertext Attack (CCA)

• The attacker is assumed to have access to the plaintexts for all ciphertexts other than the target

(5)

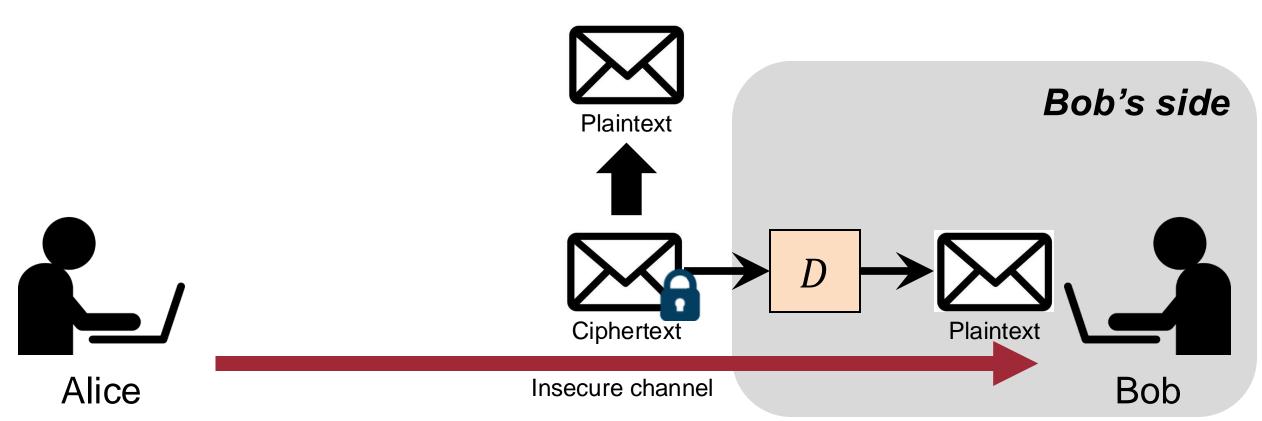


Chosen-Ciphertext Attack (CCA)

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• Can the attacker compute the key from the ciphertext?



Brute Force Search



- Always possible to simply try every key!
- Therefore, the key should be secure against exhaustive key search!

Key size (Bits)	# of alternative keys	Time required at 1 decryption/µs	Time required at 10 ⁶ decryption/µs
32	$2^{32} = 4.3 \times 10^9$	$2^{31}\mu s = 5.8 \text{ minutes}$	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	2 ⁵⁵ µs = 1,142 years	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	2^{127} µs = 5.4 × 10 ²⁴ years	5.4 \times 10 ¹⁸ years
168	$2^{168} = 3.7 \times 10^{50}$	2^{167} µs = 5.9 × 10 ³⁶ years	5.9×10^{30} years

Summary



- Classical cryptography: ad-hoc design & informal proof –Caesar's cipher, Substitution cipher, Vigenere cipher
- Modern cryptography: rigorous design & formal proof
 - -Security guarantee
 - -Threat model:
 - Ciphertext-only attack
 - Known plaintext attack
 - Chose-plaintext attack
 - Chose-ciphertext attack
 - + Brute force search

Question?